



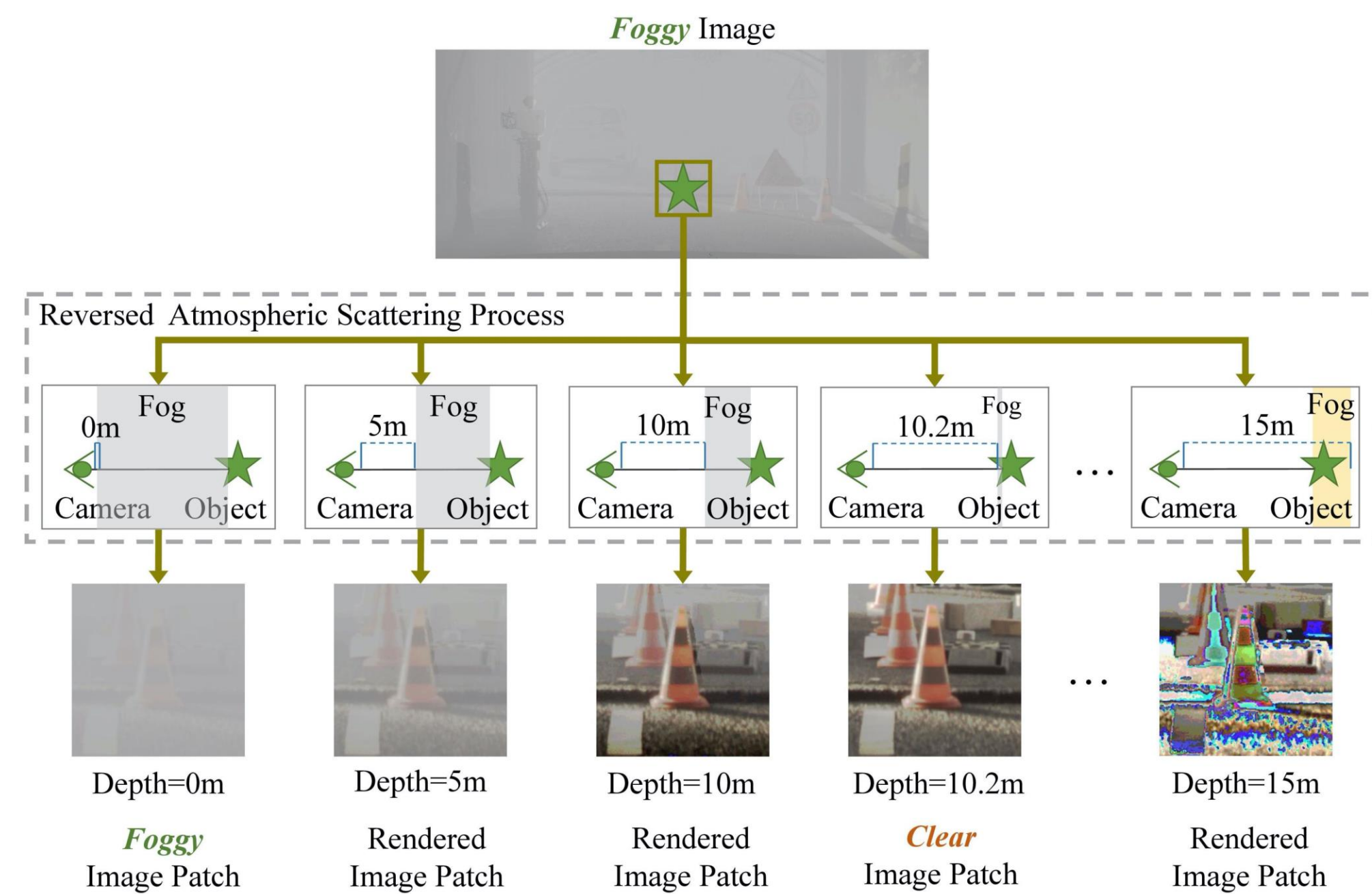
## Introduction

**Problem** Stereo matching in foggy scenes is challenging as the scattering effect of fog blurs the image and makes the matching ambiguous

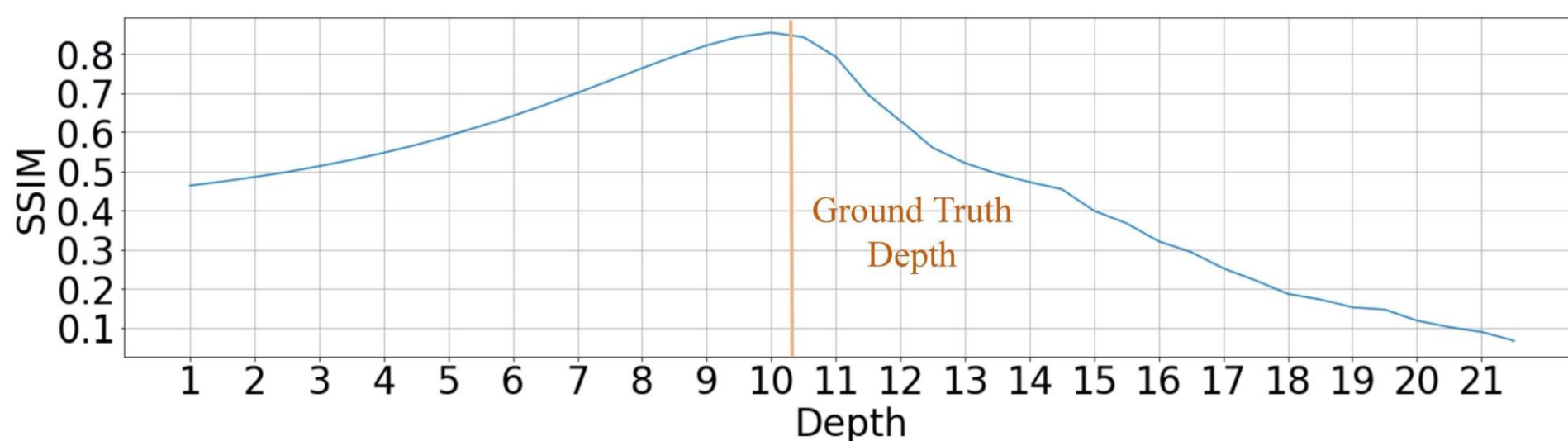
**Idea** Prior methods mainly deem fog as a noise and discard it to improve matching results. Different from them, we propose to take advantage of fog and explore depth hints for stereo matching.

**Motivation** During rendering, fog is accumulated along the light path between objects and camera following the *physical atmospheric scattering process*.

When we render the image by reversing this process, fog is removed within a selected depth range. Only the depth close to the real depth will lead to a clear image. In other words, *the quality of the rendered image indicates the correctness of depth used in the rendering.*



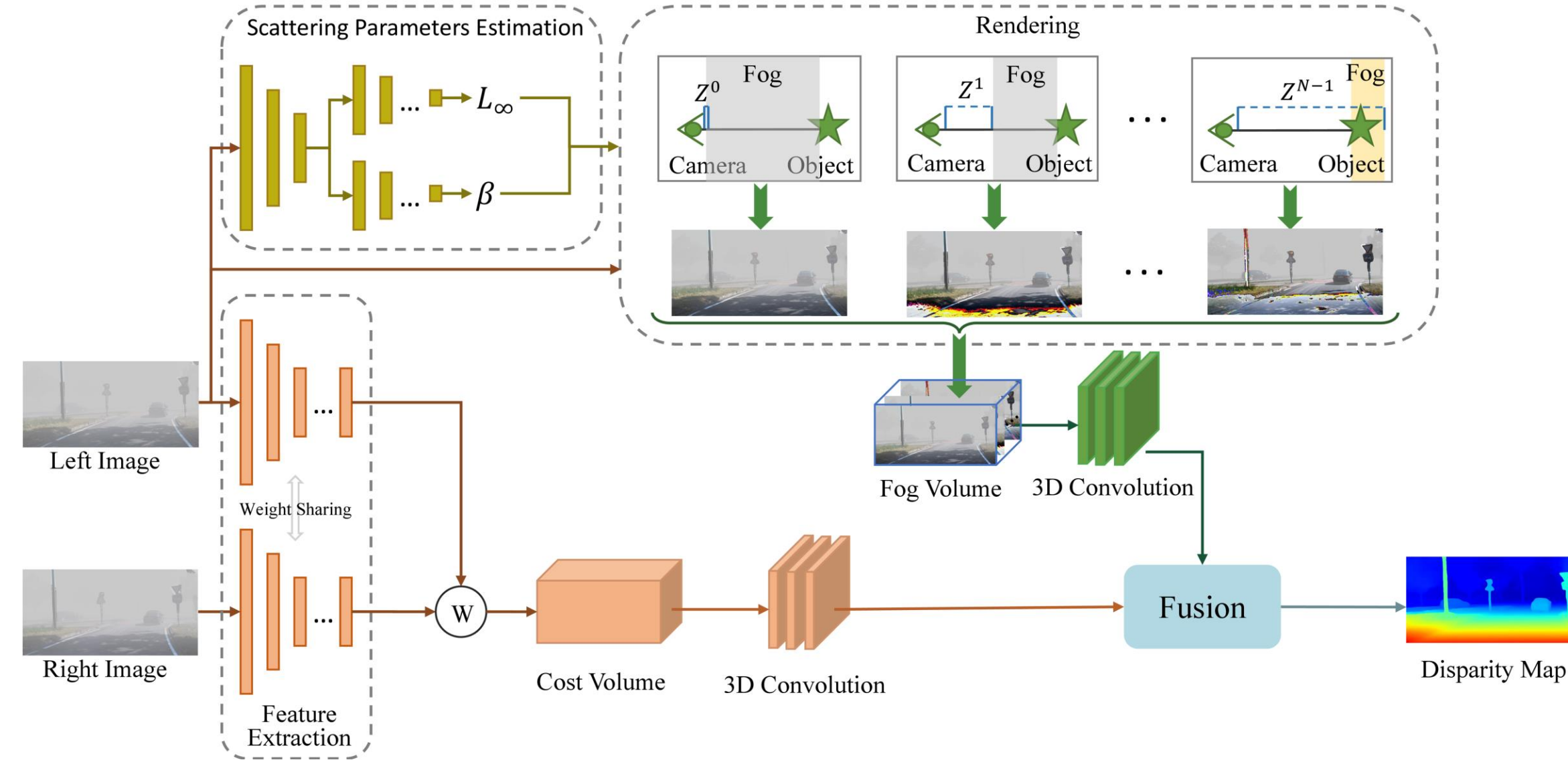
(a) The process and results of rendering.



(b) The distribution of SSIM ~ Depth.

## Method

We extract features from left and right images to build a cost volume through warping (⊗). We estimate atmospheric light  $L_\infty$  and attenuation coefficient  $\beta$  from the left image to render a series of images with different depth  $Z_i$ . The rendered images are concatenated to build fog volume, which is fused with cost volume for disparity estimation.



### Fog Volume Representation

(1) **Rendering** The atmospheric scattering effect causes the attenuation of light reflected from objects  $L_t$  and the accumulation of environmental light  $L_c$ :

$$\left. \begin{aligned} T(Z_x) &= e^{-\int_0^{Z_x} \beta(z) dz} \\ L_t(x) &= L_\infty \rho(x) T(Z_x) \\ L_c(x) &= L_\infty (1 - T(Z_x)) \end{aligned} \right\} \Rightarrow \begin{aligned} I(x) &= L_t(x) + L_c(x) \\ &= J(x)T(Z_x) + L_\infty(1 - T(Z_x)). \end{aligned}$$

The rendered image  $R$  is computed by reversing the atmospheric scattering:

$$R(x, Z_x^i) = \left( I(x) - L_\infty (1 - T(Z_x^i)) \right) / T(Z_x^i),$$

$$R(x, Z_x^i) = \ln(|I(x) - L_\infty|) + \int_0^{Z_x^i} \beta(z) dz.$$

(2) **Scattering Parameters Estimation** We set  $L_\infty$  and  $\beta$  as global parameters under the condition of one single light source and a homogeneous transporting medium.

(3) **Disparity Candidates Sampling** We sample disparity candidates  $\{D_x^i\}_{i=0}^{N-1}$  to construct cost volume, and convert them into depth  $\{Z_x^i\}_{i=0}^{N-1}$  to build the fog volume.

(4) **Rendered Images Gathering** We build the fog volume representation  $\mathcal{V}_f$  by stacking rendered images:  $\mathcal{V}_f(x, Z) = [R(x, Z_x^0), R(x, Z_x^1), \dots, R(x, Z_x^{N-1})]$ .

### Fusion

We fuse the cost volume and the fog volume with uncertainty  $\sigma$  which is the variance along disparity dimension:  $\hat{\mathcal{V}}(x, D_{\{i\}}) = [\sigma_c(x, D_i)\mathcal{V}_c(x, D_i), \sigma_f(x, D_i)\mathcal{V}_f(x, D_i)]$ .

## Results

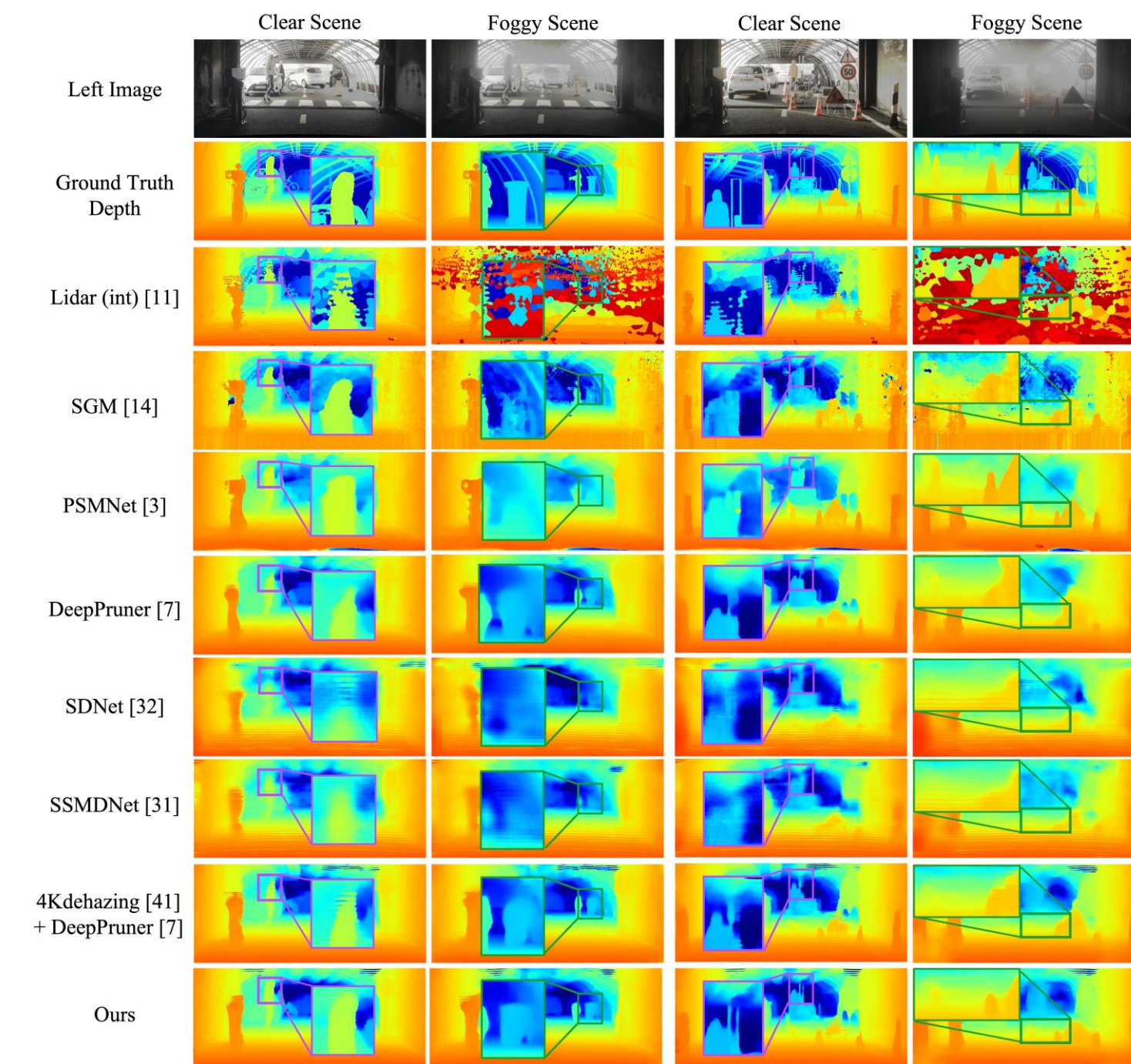
The comparison of algorithms on SceneFlow dataset. We compare the results on clear data and foggy data. \* represents our re-implementation results.

Testing	Metrics	Stereo		Joint		Sequential		Ours
		PSMNet* [3]	DeepPruner* [7]	SDNet [32]	SSMDNet [31]	4Kdehazing [41] + DeepPruner [7]		
Clear	EPE	0.99	0.98	-	-	1.19	-	<b>0.81</b>
	3px (%)	<b>4.1</b>	5.30	-	-	6.2	-	<b>4.5</b>
Foggy	EPE	1.27	3.77	2.68	2.23	1.49	-	<b>1.04</b>
	3px (%)	8.1	14.10	26.43	9.71	10.30	-	<b>7.2</b>

The comparison of algorithms on KITTI 2015 and 2012 datasets.

Methods	KITTI 2015				KITTI 2012				
	Foggy		Clear		Foggy		Clear		
	3px (%)	EPE	3px (%)	EPE	3px (%)	EPE	3px (%)	EPE	
Stereo	PSMNet* [3]	1.3	0.54	<b>1.0</b>	0.49	3.3	0.84	3.3	0.86
	DeepPruner* [7]	3.7	0.88	8.8	1.66	4.3	0.94	5.0	1.09
Joint	SDNet [32]	13.4	1.73	-	-	11.0*	1.63*	10.7*	1.60*
	SSMDNet [31]	10.8	1.23	-	-	9.7*	1.55*	9.5*	1.53*
Sequential	4Kdehazing [41] + DeepPruner [7]	7.3	0.951	<b>1.1</b>	0.49	3.2	0.91	3.2	0.89
	ours	<b>1.2</b>	<b>0.51</b>	<b>1.1</b>	<b>0.47</b>	<b>2.7</b>	<b>0.77</b>	<b>2.7</b>	<b>0.78</b>

The visualization of depth map on PixelAccurateDeth dataset with real foggy scenes.



The visualization of error rate (EPE) distribution over the depth and the fog thickness.

